## Numpy multidimensional arrays

By examples
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## Creation:

```
import numpy as np
a = np.array([[ 1, 2, 3, 4],
    [ 5, 6, 7, 8],
    [ 9, 10, 11, 12]])
```


## Dimension and shape:

| print (a.ndim) | 2 |  |
| :--- | :--- | :--- |
| print (a.shape) | $(3,4)$ | $\# 3$ rows, 4 columns |
| print (a.size) | 12 | $\# 12$ elements |

First dimension: rows, second dimension: columns

## Reshape:

| ```b = a.reshape(4,3) print(b)``` |  |
| :---: | :---: |

This might not be what you wanted
The reference trap:

| $\mathbf{c}=\mathbf{a}$ |
| :--- | :--- |
| $c[0,0]=314$ |
| $\operatorname{print(a)}$ |
| $\operatorname{print(c)}$ |$\quad\left[\begin{array}{lrrr}{[314} & 2 & 3 & 4\end{array}\right]$

Setting one or more elements of the copy c to new values, changes not only the copied array c, but also the original array a.
Take care:
The arrays a and c reference the same array, after c = a.
So if an element of c is changed, the same element of a is also changed.
(This is true for other kinds of lists also, in general for mutable objects)
If you do not want this, use the copy function:

| c $=$ a.copy () |
| :--- | :--- |
| c[0,0] $=512$ |
| print(a) |
| print (c) |$\quad\left[\begin{array}{lrrr}{[314} & 2 & 3 & 4\end{array}\right]$

(Remember that $\mathrm{a}[0,0]$ was changed in the previous example)

## Indexing and slicing

Remember that all indexing starts with 0 !
So the $2^{\text {nd }}$ row for example has index 1.

Let's begin with the same matrix a:
import numpy as np
a = np.array $\left(\left[\begin{array}{l}1, ~ 2, ~ 3, ~ 4] \\ \hline\end{array}\right.\right.$
$\left[\begin{array}{lrrr}5, & 6, & 8\end{array}\right]$,
$[9,10,11,12]])$

## Get the second row:

| $\mathrm{b}=\mathrm{a}[1]$ |
| :--- | :--- | :--- |
| $\operatorname{print}(\mathrm{b})$ |$\quad\left[\begin{array}{llll}5 & 6 & 7 & 8\end{array}\right] \quad$.

Get the last row:

| $c=a[-1]$ | $\left[\begin{array}{llll}9 & 10 & 11 & 12\end{array}\right]$ |
| :--- | :--- | :--- | :--- | :--- | :--- |

Get the element in the 3rd row and 2nd column:

| $\mathrm{d}=\mathrm{a}[2,1]$ | 10 |
| :--- | :--- |

Indexing goes by [row, column]
By the way, another valid syntax would be $d=a[2][1]$

## Get the 3rd column:

| $\mathrm{e}=\mathrm{a}[:, 2]$ | $\left[\begin{array}{lll}3 & 7 & 11\end{array}\right]$ |
| :--- | :--- |

Indexing goes by [row, column] and ":" means: all in this, so all rows of column 2

Get a submatrix consisting of $2^{\text {nd }}$ and $3^{\text {rd }}$ columns:
$\left.\mathrm{f}=\mathrm{a}[:, 1: 3] \quad\left[\begin{array}{ccc}{\left[\begin{array}{ll}2 & 3\end{array}\right]} \\ {[ } & 6 & 7 \\ {[10} & 11\end{array}\right]\right]$

This gives all rows of the columns with index 1 and 2 (remember that " $1: 3$ " means
"from 1 to $3-1=2$ " !
( as 1:3 includes 1 , but excludes 3, one of the weirdnesses of Python)

## Floating point arrays

## The integer trap:

All the above examples were done with integers. Numpy has looked at the defined array a and found it all integers, so the resulting arrays also were integer arrays.

Even an assignment like
$\mathrm{a}[0,0]=3.14$
would not change the type of the array, the result would be a cast of 3.14 to the ineger value 3 .

Defining a floating point array:


Even if only one element is a floating point number, Numpy sets all elements to floating point, as can be seen in the result.

## Other Numpy functions

## Make an array from lists and / or arrays:

| import numpy as np | ( (3.14, 2, 5), [2, 3, 4]) |
| :---: | :---: |
| $\mathrm{l1}=(3.14,2,5)$ |  |
| $12=[2,3,4]$ |  |
| $\mathrm{l}=\mathrm{l} 1, \quad \mathrm{l} 2$ | [ $\left[\begin{array}{llll}3.14 & 2 & 5\end{array}\right]$ |
| $\mathrm{a}=\mathrm{np} . \operatorname{asarray(l)}$ | $\left[\begin{array}{llll}2 . & 3 . & 4 .\end{array}\right]$ |
| print(a) | [2. 3. 4. ]] |

## Make zeros array:

```
# one dimensional:
z = np.zeros(5)
print(z)
# 2 dimensional
z2 = np.zeros((2,3))
print(z2)
```


## Make an array of evenly spaced numbers:

Example: 5 values between 2 and 3

| $l=n p . \operatorname{linspace}(2,3,5)$ | $[2$. | 2.25 | 2.5 | 2.75 | 3. | $]$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Operations on arrays

Operations are done element wise.

```
import numpy as np
a = np.array([[ 1, 2, 3, 4],
    [ 5, 6, 7, 8],
    [ 9, 10, 11, 12]])
b = a * 2
print(b)
c = a + b
print(c)
```



This is also true for multiplication and division.
Functions can directly operate on arrays:

| $d=n p . \sin (a)$ |
| :--- | :---: | :---: | :---: | :---: |
| $p r i n t(d)$ |$\quad\left[\begin{array}{cccc}{\left[\begin{array}{ll}0.84147098 & 0.90929743\end{array}\right.} & 0.14112001 & -0.7568025\end{array}\right]$

Calculations with constants are also done elementwise:

| $e=a+5$ |
| :--- | :--- |
| $p r i n t(e)$ | \left\lvert\,\(\left[$$
\begin{array}{rrrr}{\left[\begin{array}{rrrr}6 & 7 & 8 & 9\end{array}
$$\right]} <br>

{[10} \& 11 \& 12 \& 13 <br>
{[14} \& 15 \& 16 \& 17\end{array}\right]\right.\)

## Mathematical Matrix operations

Matrix multiplication $\rightarrow$ dot function

```
import numpy as np
a = np.array([[[1, 2 ],
    [ 3, 4]]])
b = np.array([[5, 6],
    [7, 8]])
c = np.dot(a,b)
print(c)
```

```
[[\begin{array}{lll}{19}&{22]}\end{array}]
```

    [43 50]]